

Name:

Class Period:

## First Semester Day 6 Review: Arithmetic Sequences

### Guided Notes

#### Arithmetic Sequences

##### Definitions

- ↳ An ordered list of number is called a sequence.
- ↳ The number in a sequence are terms.
- ↳ An arithmetic sequence is a sequence in which the difference between terms is constant.
- ↳ The difference between consecutive terms in an arithmetic sequence is called the common difference.

##### Explicit Formula

Two pieces of information is needed to write an explicit formula for an arithmetic sequence:

- ↳ First term ( $a_1$ )
- ↳ Common difference ( $d$ )

Enter this information for the appropriate values in the following formula:

$$a_n = a_1 + (n - 1)d$$

Example 1

Write the following numbers as a sequence: 1, -1, 5, 3, 2. Is this an arithmetic sequence? Explain your reasoning.

Sequence -1, 1, 2, 3, 5

NO, there is no common difference

Example 2

Write the following numbers as a sequence and write the common difference: 1, 5, 7, 9, 3.

Sequence 1, 3, 5, 7, 9      Common difference = 2

Example 3

Identify the following values.

$$a_1 = 1$$

$$a_2 = 3$$

$$a_3 = 5$$

$$a_4 = 7$$

$$a_5 = 9$$

$$d = 2$$

Example 4

Write the explicit formula for the sequence.

$$a_n = a_1 + (n-1)d = 1 + (n-1)2 = 1 + 2n - 2 = 2n - 1$$

Example 5

Rewrite the explicit formula using function notation and let the function be called  $f(n)$ .

$$f(n) = 2n - 1$$

Example 6

Use the explicit formula or function to evaluate  $f(10)$ .

$$f(10) = 2(10) - 1 = 20 - 1 = 19$$

**Classwork**

Problem 1

Write the following numbers as a sequence: 72, 4, 21, 7, 0. Is this an arithmetic sequence? Explain your reasoning.

Sequence 0, 4, 7, 21, 72

No, there is no common difference

Problem 2

Write the following numbers as a sequence and write the common difference: 15, 5, 20, 10.

Sequence 5, 10, 15, 20

Common difference = 5

Problem 3

Identify the following values.

$$a_1 = 5$$

$$a_2 = 10$$

$$a_3 = 15$$

$$a_4 = 20$$

$$d = 5$$

Problem 4

Write the explicit formula for the sequence.

$$a_n = a_1 + (n-1)d = 5 + (n-1)5 = 5 + 5n - 5 = 5n$$

Problem 5

Rewrite the explicit formula using function notation and let the function be called  $f(n)$ .

$$f(n) = 5n$$

Problem 6

Use the explicit formula or function to evaluate  $f(8)$ .

$$f(8) = 5(8) = 40$$